## BUEC 333: Assignment 3

## 8 points for this section

- 1) [Midterm, Spring 2009] (1 point) The power of a test is the probability that you:
  - a) reject the null when it is true
  - b) fail to reject the null when it is false
  - c) reject the null when it is false
  - d) fail to reject the null when it is true
  - e) none of the above
- 2) [Midterm, Spring 2009] (**1 point**) Suppose you compute a sample statistic *q* to estimate a population quantity *Q*. Which of the following four statements is/are **false**?
  - [1] the variance of Q is zero
  - [2] if q is an unbiased estimator of Q, then q = Q
  - [3] if q is an unbiased estimator of Q, then q is the mean of the sampling distribution of Q [4] a 95% confidence interval for q contains Q with 95% probability
  - a) 2 only
  - b) 3 only
  - c) 2 and 3
  - d) 2, 3, and 4
  - e) 1, 2, 3, and 4
- 3) [Midterm, Spring 2009] (**1 point**) Suppose you want to test the following hypothesis at the 10% level of significance:

$$H_0: \mu = \mu_0$$

 $H_1: \mu \neq \mu_0$ 

Which of the following statements is/are true?

- a) the probability of a Type I error is 0.05
- b) the probability of a Type I error is 0.10
- c) the probability of a Type II error is 0.90
- d) the probability of a Type II error is 0.10
- e) none of the above
- 4) (4 points) Suppose you collect the following data that you know are a random sample from a  $N(\mu,\sigma^2)$  population:

4.37 6.99 7.85 2.60 3.34 5.94 4.21 5.99 8.53 4.92

a) Compute the t-statistic for testing the hypothesis:

$$H_0: \mu = 4$$
  
 $H_1: \mu \neq 4$ 

- i) mu-hat=5.474; E[V(mu-hat)]=s2=V(x)/(n-1)=3.74/9=0.41; mu-hat-4/sqrt(V(mu-hat))=1.474/sqrt(0.41)=2.28 (2 points)
- b) What is the sampling distribution of the test statistic you computed in part a? t with 9 df (1 point)
- c) Can you reject the null hypothesis of part a at the 5% level of significance? 5% crit with 9 df is 2.26. So, we reject because 2.28>2.26. (1 point)
- 5) (1 point) In the linear regression model,  $R^2$  measures
  - a) The proportion of variation in Y explained by X

- b) The proportion of variation in *X* explained by *Y*c) The proportion of variation in *Y* explained by *X*, adjusted for the number of independent variables
- d) The proportion of variation in *X* explained by *Y*, adjusted for the number of independent variables
- e) None of the above

- 6) **[10 points for this section]** EVIEWS PART: Read Pendakur, Krishna and Ravi Pendakur, 2010, "Colour By Numbers: Minority Earnings Disparity 1995-2005", forthcoming, <u>Journal of Intenational Migration and Integration</u>, linked on the course website.
  - a) In your sample of data from people living in Greater Vancouver, select a sample which corresponds to the sample selected for regression estimation by Pendakur and Pendakur (2010). Note that while they use the entire sample of the long-form census file, you use only about one in seven observations from that file: the long-forms cover 20% of the population, but the public-use data that you have cover only 3% of the population. You will use this sample for all the questions below, too. How many observations do you have? Make a table showing the average earnings of white, visible minority and Aboriginal men and women (6 types) in this sample.

# 1 point: 13199 cases (if they're close, they get 1 point) THE KEY IS TO DROP MISSINGS

these numbers are from descriptive statistics, manipulating the sample for each number

- b) Make a table showing the standard errors of the sample means you reported in part b. These standard errors equal the square-root of the variance of sampling distributions of the sample means in part b.
- 7) these numbers are from descriptive statistics, manipulating the sample for each number
  - a) these numbers are std dev/root-n, both of which are given in the descriptive statistics.
  - b) 1 point for sample means that are close; 1 point for std errs that are close.

|        |          |          |     | siu        |
|--------|----------|----------|-----|------------|
|        | mean     | std dev  | n   | dev/rootn  |
| wt-wom | 38534.84 | 30043.27 | 565 | 2 399.619  |
| wt-men | 64084.8  | 78456.46 | 584 | 7 1026.035 |
| vm-wom | 39734.27 | 31343.37 | 62  | 6 1252.733 |
| vm-men | 53484.13 | 65537.1  | 66  | 9 2533.811 |
| ab-wom | 40185.79 | 29223.81 | 18  | 3 2160.286 |
| ab-men | 31705.19 | 30444.25 | 22  | 2 2043.284 |

c) Make a table showing the difference between the sample mean of white and visible minority and white and Aboriginal earnings for men and women (4 comparisons). Include the standard errors of these differences in this table.

The key here is to note (from the formula for variance) that the variance of a difference of two sample means is the sum of their variances, and the std err is the square root of that. see next table

- d) Construct test statistics for 4 hypotheses: the average earnings of visible minority men in the population is lower than that of white men; the average earnings of Aboriginal men in the population is lower than that of white men; the average earnings of visible minority women in the population is lower than that of white women; and the average earnings of Aboriginal women in the population is lower than that of white women.
- 8) 1 point for std errs that are close; 1 point for test stats that are close; 1 point for correct interpretation of tests

|        |      |          |              |          | test     |
|--------|------|----------|--------------|----------|----------|
|        | Diff |          | std err diff |          | stat     |
| vm-wm  |      | 1199.43  |              | 1314.928 | 0.912164 |
| vm-men |      | -10600.7 |              | 2733.669 | -3.87782 |

| Abwom  | 1650.95  | 2196.937 | 0.751478 |
|--------|----------|----------|----------|
| ab-men | -32379.6 | 2286.429 | -14.1617 |

#### for men, these minorities have lower average earnings.

 a) Run regressions like those in Table 2, corresponding to regressions controlling for personal characteristics only in Vancouver in 2005 (2006 microdata are about 2005 earnings). Be sure that you get the dependent variable correct. Report the output for the visible minority and Aboriginal coefficients only.

## MEN

Dependent Variable: LOG(WAGES) Method: Least Squares Date: 11/12/10 Time: 14:41 Sample: 1 56529 IF AGEGRP>8 AND AGEGRP<17 AND WAGES>100 AND SEX=2 AND CITIZEN=1 AND WAGES<8000000 Included observations: 6708

| C 9.941972 0.065480 151.8332 0.000   VISMIN<13 -0.039790 0.038440 -1.035122 0.300   ABOID<6 -0.230604 0.068768 -3.353367 0.000   AGEGRP=10 0.309813 0.041488 7.467624 0.000   AGEGRP=11 0.386448 0.042412 9.111749 0.000   AGEGRP=12 0.485940 0.043395 11.19814 0.000   AGEGRP=13 0.566416 0.044362 12.76799 0.000   AGEGRP=14 0.473529 0.046511 10.18092 0.000 | Variable           | Coefficient                | Std. Error            | t-Statistic        | Prob.    |
|---|--------------------|----------------------------|-----------------------|--------------------|----------|
| VISMIN<13 -0.039790 0.038440 -1.035122 0.300   ABOID<6  | С                  | 9.941972                   | 0.065480              | 151.8332           | 0.0000   |
| ABOID<6 -0.230604 0.068768 -3.353367 0.000   AGEGRP=10 0.309813 0.041488 7.467624 0.000   AGEGRP=11 0.386448 0.042412 9.111749 0.000   AGEGRP=12 0.485940 0.043395 11.19814 0.000   AGEGRP=13 0.566416 0.044362 12.76799 0.000   AGEGRP=14 0.473529 0.046511 10.18092 0.000   | VISMIN<13          | -0.039790                  | 0.038440              | -1.035122          | 0.3006   |
| AGEGRP=10 0.309813 0.041488 7.467624 0.000   AGEGRP=11 0.386448 0.042412 9.111749 0.000   AGEGRP=12 0.485940 0.043395 11.19814 0.000   AGEGRP=13 0.566416 0.044362 12.76799 0.000   AGEGRP=14 0.473529 0.046511 10.18092 0.000  | ABOID<6            | -0.230604                  | 0.068768              | -3.353367          | 0.0008   |
| AGEGRP=11 0.386448 0.042412 9.111749 0.000   AGEGRP=12 0.485940 0.043395 11.19814 0.000   AGEGRP=13 0.566416 0.044362 12.76799 0.000   AGEGRP=14 0.473529 0.046511 10.18092 0.000   AGEGRP=14 0.473529 0.046511 10.18092 0.000  | AGEGRP=10          | 0.309813                   | 0.041488              | 7.467624           | 0.0000   |
| AGEGRP=12 0.485940 0.043395 11.19814 0.000   AGEGRP=13 0.566416 0.044362 12.76799 0.000   AGEGRP=14 0.473529 0.046511 10.18092 0.000  | AGEGRP=11          | 0.386448                   | 0.042412              | 9.111749           | 0.0000   |
| AGEGRP=13 0.566416 0.044362 12.76799 0.000   AGEGRP=14 0.473529 0.046511 10.18092 0.000   | AGEGRP=12          | 0.485940                   | 0.043395              | 11.19814           | 0.0000   |
| AGEGRP=14 0.473529 0.046511 10.18092 0.000  | AGEGRP=13          | 0.566416                   | 0.044362              | 12.76799           | 0.0000   |
|   | AGEGRP=14          | 0.473529                   | 0.046511              | 10.18092           | 0.0000   |
| AGEGRP=15 0.375384 0.049936 7.517266 0.000  | AGEGRP=15          | 0.375384                   | 0.049936              | 7.517266           | 0.0000   |
| AGEGRP=16 -0.020625 0.061228 -0.336847 0.736  | AGEGRP=16          | -0.020625                  | 0.061228              | -0.336847          | 0.7362   |
| HDGREE=2 0.227064 0.044155 5.142462 0.000   | HDGREE=2           | 0.227064                   | 0.044155              | 5.142462           | 0.0000   |
| HDGREE=3 0.144260 0.057971 2.488471 0.012   | HDGREE=3           | 0.144260                   | 0.057971              | 2.488471           | 0.0129   |
| HDGREE=4 0.326140 0.055970 5.826997 0.000   | HDGREE=4           | 0.326140                   | 0.055970              | 5.826997           | 0.0000   |
| HDGREE=5 0.183697 0.075001 2.449266 0.014   | HDGREE=5           | 0.183697                   | 0.075001              | 2.449266           | 0.0143   |
| HDGREE=6 0.358519 0.050980 7.032498 0.000   | HDGREE=6           | 0.358519                   | 0.050980              | 7.032498           | 0.0000   |
| HDGREE=7 0.376088 0.061504 6.114836 0.000   | HDGREE=7           | 0.376088                   | 0.061504              | 6.114836           | 0.0000   |
| HDGREE=8 0.311281 0.064569 4.820913 0.000   | HDGREE=8           | 0.311281                   | 0.064569              | 4.820913           | 0.0000   |
| HDGREE=9 0.510465 0.047439 10.76043 0.000   | HDGREE=9           | 0.510465                   | 0.047439              | 10.76043           | 0.0000   |
| HDGREE=10 0.476429 0.083294 5.719855 0.000  | HDGREE=10          | 0.476429                   | 0.083294              | 5.719855           | 0.0000   |
| HDGREE=11 1.102464 0.137275 8.031053 0.000  | HDGREE=11          | 1.102464                   | 0.137275              | 8.031053           | 0.0000   |
| HDGREE=12 0.623808 0.063306 9.853824 0.000  | HDGREE=12          | 0.623808                   | 0.063306              | 9.853824           | 0.0000   |
| HDGREE=13 0.774046 0.115171 6.720865 0.000  | HDGREE=13          | 0.774046                   | 0.115171              | 6.720865           | 0.0000   |
| HDGREE=88 0.411254 0.347135 1.184709 0.236  | HDGREE=88          | 0.411254                   | 0.347135              | 1.184709           | 0.2362   |
| MARST=2 0.216753 0.043658 4.964759 0.000  | MARST=2            | 0.216753                   | 0.043658              | 4.964759           | 0.0000   |
| MARST=3 0.005277 0.074057 0.071258 0.943  | MARST=3            | 0.005277                   | 0.074057              | 0.071258           | 0.9432   |
| MARST=4 -0.191438 0.047174 -4.058091 0.000  | MARST=4            | -0.191438                  | 0.047174              | -4.058091          | 0.0001   |
| MARST=5 -0.097890 0.161492 -0.606162 0.544  | MARST=5            | -0.097890                  | 0.161492              | -0.606162          | 0.5444   |
| KOL=2 -0.169922 0.525802 -0.323167 0.746  | KOL=2              | -0.169922                  | 0.525802              | -0.323167          | 0.7466   |
| KOL=3 -0.077730 0.038501 -2.018911 0.043  | KOL=3              | -0.077730                  | 0.038501              | -2.018911          | 0.0435   |
| R-squared 0.139391 Mean dependent var 10.6356   | R-squared          | 0.139391                   | Mean depend           | lent var           | 10.63560 |
| Adjusted R-squared 0.135783 S.D. dependent var 0.97628  | Adjusted R-squared | djusted R-squared 0.135783 |                       | S.D. dependent var |          |
| S.E. of regression 0.907588 Akaike info criterion 2.64826   | S.E. of regression | 0.907588                   | Akaike info criterion |                    | 2.648261 |
| Sum squared resid 5501.596 Schwarz criterion 2.67770  | Sum squared resid  | 5501.596                   | Schwarz crite         | rion               | 2.677706 |
| Log likelihood -8853.267 Hannan-Quinn criter. 2.65842   | Log likelihood     | -8853.267                  | Hannan-Quin           | n criter.          | 2.658429 |
| F-statistic 38.63503 Durbin-Watson stat 2.02339   | F-statistic        | 38.63503                   | Durbin-Watso          | on stat            | 2.023390 |
| Prob(F-statistic) 0.000000  | Prob(F-statistic)  | 0.000000                   |                       |                    |          |

# WOMEN

Dependent Variable: LOG(WAGES) Method: Least Squares Date: 11/12/10 Time: 14:42 Sample: 1 56529 IF AGEGRP>8 AND AGEGRP<17 AND WAGES>100 AND SEX=1 AND CITIZEN=1 AND WAGES<8000000 Included observations: 6508

| Variable           | Coefficient | Std. Error            | t-Statistic | Prob.    |
|--------------------|-------------|-----------------------|-------------|----------|
| С                  | 9.427923    | 0.068987              | 136.6629    | 0.0000   |
| VISMIN<13          | 0.088903    | 0.040238              | 2.209420    | 0.0272   |
| ABOID<6            | -0.151119   | 0.064010              | -2.360854   | 0.0183   |
| AGEGRP=10          | 0.205175    | 0.042687              | 4.806477    | 0.0000   |
| AGEGRP=11          | 0.294197    | 0.044133              | 6.666189    | 0.0000   |
| AGEGRP=12          | 0.483487    | 0.044757              | 10.80258    | 0.0000   |
| AGEGRP=13          | 0.527377    | 0.044440              | 11.86718    | 0.0000   |
| AGEGRP=14          | 0.544731    | 0.047376              | 11.49810    | 0.0000   |
| AGEGRP=15          | 0.408922    | 0.051016              | 8.015549    | 0.0000   |
| AGEGRP=16          | 0.020519    | 0.062757              | 0.326963    | 0.7437   |
| HDGREE=2           | 0.335415    | 0.053664              | 6.250289    | 0.0000   |
| HDGREE=3           | 0.283880    | 0.070474              | 4.028155    | 0.0001   |
| HDGREE=4           | 0.345029    | 0.109560              | 3.149238    | 0.0016   |
| HDGREE=5           | 0.320319    | 0.064221              | 4.987739    | 0.0000   |
| HDGREE=6           | 0.405661    | 0.058203              | 6.969763    | 0.0000   |
| HDGREE=7           | 0.583164    | 0.068969              | 8.455416    | 0.0000   |
| HDGREE=8           | 0.517791    | 0.067027              | 7.725157    | 0.0000   |
| HDGREE=9           | 0.696710    | 0.056237              | 12.38877    | 0.0000   |
| HDGREE=10          | 0.648735    | 0.079914              | 8.117956    | 0.0000   |
| HDGREE=11          | 0.762487    | 0.176601              | 4.317575    | 0.0000   |
| HDGREE=12          | 0.851479    | 0.068188              | 12.48724    | 0.0000   |
| HDGREE=13          | 1.209336    | 0.185073              | 6.534382    | 0.0000   |
| HDGREE=88          | 0.246933    | 0.331299              | 0.745347    | 0.4561   |
| MARST=2            | -0.010021   | 0.037827              | -0.264930   | 0.7911   |
| MARST=3            | -0.061969   | 0.063042              | -0.982982   | 0.3257   |
| MARST=4            | 0.036099    | 0.042848              | 0.842492    | 0.3995   |
| MARST=5            | -0.087644   | 0.094282              | -0.929585   | 0.3526   |
| KOL=2              | 0.699086    | 0.930578              | 0.751239    | 0.4525   |
| KOL=3              | -0.054751   | 0.037589              | -1.456558   | 0.1453   |
| KOL=4              | -0.613353   | 0.927668              | -0.661178   | 0.5085   |
| R-squared          | 0.083489    | Mean depend           | lent var    | 10.21663 |
| Adjusted R-squared | 0.079386    | S.D. dependent var    |             | 0.964859 |
| S.E. of regression | 0.925769    | Akaike info criterion |             | 2.688215 |
| Sum squared resid  | 5551.956    | Schwarz criterion     |             | 2.719472 |
| Log likelihood     | -8717.450   | Hannan-Quinn criter.  |             | 2.699025 |
| F-statistic        | 20.34866    | Durbin-Watson stat 2  |             | 2.101746 |
| Prob(F-statistic)  | 0.000000    |                       |             |          |

### 1 point for regression output 1 point for tests

b) Test the hypothesis that the mean log-earnings of visible minority men is lower than that of white men, and similarly for Aboriginal men, and similarly for women.

- c) vm men not significantly lower; vm women not significantly lower; aboriginal men significantly lower; aboriginal women significantly lower. not that vm women earn significantly more.
- d) How do your results differ from Pendakur and Pendakur (2010)? Why do they differ?
- e) 1 point: not identical numbers because different sample, with 1/7 the number of cases. they could see the negative for vm men that is too small to see with only 1/7 the data.
- f) Table 2 also considers regressions that control for work characteristics. How does their argument for the difference between these two variables connect with missing variables bias?

1 point: work characteristics are missing variables in the regression above. if they're correlated with vm or aboriginal status, then that correlation biases the coefficient.